

1. Let $A = [a_{ij}], B = [b_{ij}]$ are two 3×3 matrices such that $b_{ij} = \lambda^{i+j-2}a_{ij}$ & $|B| = 81$. Find $|A|$ if $\lambda = 3$.
- A) $\frac{1}{9}$ B) 3 C) $\frac{1}{81}$ D) $\frac{1}{27}$

Ans. A

Sol. $|B| = \begin{vmatrix} b_{11} & b_{12} & b_{13} \\ b_{21} & b_{22} & b_{23} \\ b_{31} & b_{32} & b_{33} \end{vmatrix} = \begin{vmatrix} 3^0 a_{11} & 3^1 a_{12} & 3^2 a_{13} \\ 3^1 a_{21} & 3^2 a_{22} & 3^3 a_{23} \\ 3^2 a_{31} & 3^3 a_{32} & 3^4 a_{33} \end{vmatrix} \Rightarrow 81 = 3^3 \cdot 3 \cdot 3^2 |A| \Rightarrow 3^4 = 3^6 |A| \Rightarrow |A| = \frac{1}{9}$

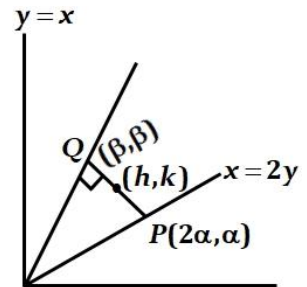
2. From any point P on the line $x = 2y$ perpendicular is drawn on $y = x$. Let foot of perpendicular is Q . Find the locus of mid point of PQ .
- A) $2x = 3y$ B) $5x = 7y$ C) $3x = 2y$ D) $7x = 5y$

Ans. B

Sol. Slope of $PQ = \frac{k-\alpha}{h-2\alpha} = -1$
 $\Rightarrow k - \alpha = -h + 2\alpha$
 $\Rightarrow \alpha = \frac{h+k}{3}$ (1)

Also $2h = 2\alpha + \beta$
 $2k = \alpha + \beta$
 $\Rightarrow 2h = \alpha + 2k$
 $\Rightarrow \alpha = 2h - 2k$ (2)

from (1) & (2)
 $\frac{h+k}{3} = 2(h-k)$
 so locus is $6x - 6y = x + y \Rightarrow 5x = 7y$



3. Pair of tangents are drawn from origin to the circle $x^2 + y^2 - 8x - 4y + 16 = 0$ then square of length of chord of contact is
- A) $\frac{64}{5}$ B) $\frac{24}{5}$ C) $\frac{8}{5}$ D) $\frac{8}{13}$

Ans. A

Sol. $L = \sqrt{S_1} = \sqrt{16} = 4$
 $R = \sqrt{16 + 4 - 16} = 2$
 Length of chord of contact $= \frac{2LR}{\sqrt{L^2 + R^2}} = \frac{2 \times 4 \times 2}{\sqrt{16 + 4}} = \frac{16}{\sqrt{20}}$
 Square of length of chord of contact $= \frac{64}{5}$

4. Contrapositive of if $A \subset B$ and $B \subset C$ then $C \subset D$
- A) $C \not\subset D$ or $A \not\subset B$ or $B \not\subset C$ B) $C \subset D$ and $A \not\subset B$ or $B \not\subset C$
 C) $C \subset D$ or $A \not\subset B$ and $B \not\subset C$ D) $C \subset D$ or $A \not\subset B$ or $B \not\subset C$

Ans. D

Sol. Let $P = A \subset B, Q = B \subset C, R = C \subset D$
 Contrapositive of $(P \wedge Q) \rightarrow R$ is $\sim R \rightarrow \sim (P \wedge Q)$
 $R \vee (\sim P \vee \sim Q)$

5. Let $y(x)$ is solution of differential equation $(y^2 - x) \frac{dy}{dx} = 1$ and $y(0) = 1$, then find the value of x where curve cuts the x -axis
- A) $2 - e$ B) $2 + e$ C) 2 D) e

Ans. A

Sol. $\frac{dx}{dy} + x = y^2$

I.F. = $e^{\int 1 \cdot dy} = e^y$

$x \cdot e^y = \int y^2 \cdot e^y \cdot dy$

$= y^2 \cdot e^y - \int 2y \cdot e^y \cdot dy$

$\Rightarrow y^2 e^y - 2(y \cdot e^y - e^y) + c$

$x \cdot e^y = y^2 e^y - 2y e^y + 2e^y + c$

$x = y^2 - 2y + 2 + c \cdot e^{-y}$

$x = 0, y = 1$

$0 = 1 - 2 + 2 + \frac{c}{e}$

$c = -e$

$y = 0, x = 0 - 0 + 2 + (-e)(e^{-0})$

$x = 2 - e$

6. Let θ_1 and θ_2 (where $\theta_1 < \theta_2$) are two solutions of $2 \cot^2 \theta - \frac{5}{\sin \theta} + 4 = 0, \theta \in [0, 2\pi)$ then $\int_{\theta_1}^{\theta_2} \cos^2 3\theta d\theta$ is equal to

A) $\frac{\pi}{3}$

B) $\frac{2\pi}{3}$

C) $\frac{\pi}{9}$

D) $\frac{\pi}{3} + \frac{1}{6}$

Ans. A

Sol. $2 \cot^2 \theta - \frac{5}{\sin \theta} + 4 = 0$

$\frac{2 \cos^2 \theta}{\sin^2 \theta} - \frac{5}{\sin \theta} + 4 = 0$

$2 \cos^2 \theta - 5 \sin \theta + 4 \sin^2 \theta = 0, \sin \theta \neq 0$

$2 \sin^2 \theta - 5 \sin \theta + 2 = 0$

$(2 \sin \theta - 1)(\sin \theta - 2) = 0$

$\sin \theta = \frac{1}{2}$

$\theta = \frac{\pi}{6}, \frac{5\pi}{6}$

$\therefore \int_{\pi/6}^{5\pi/6} \cos^2 3\theta d\theta = \int_{\pi/6}^{5\pi/6} \frac{1 + \cos 6\theta}{2} d\theta$

$= \frac{1}{2} \left[\theta + \frac{\sin 6\theta}{6} \right]_{\pi/6}^{5\pi/6} = \frac{1}{2} \left[\frac{5\pi}{6} - \frac{\pi}{6} + \frac{1}{6}(0 - 0) \right] = \frac{1}{2} \cdot \frac{4\pi}{6} = \frac{\pi}{3}$

7. Let $3 + 4 + 8 + 9 + 13 + 14 + 18 + \dots + 40$ terms = S . If $S = (102)m$ then $m =$

A) 20

B) 25

C) 10

D) 5

Ans. A

Sol. $S = \underbrace{3+4} + \underbrace{8+9} + \underbrace{13+14} + \underbrace{18+19} \dots 40$ terms

$S = 7 + 17 + 27 + 37 + 47 + \dots 20$ terms

$S_{40} = \frac{20}{2} [2 \times 7 + (19)10] = 10[14 + 190] = 10[2040] = (102)(20)$

$\Rightarrow m = 20$

8. If $({}^{36}C_{r+1}) \times (k^2 - 3) = {}^{35}C_r \cdot 6$, then number of ordered pairs (r, k) are (where $k \in I$).

A) 6

B) 2

C) 3

D) 4

Ans. D

Sol. $\frac{{}^{36}C_{r+1}}{r+1} \times \frac{{}^{35}C_r}{r} (k^2 - 3) = \frac{{}^{35}C_r}{r}$

$k^2 - 3 = \frac{r+1}{6} \Rightarrow k^2 = 3 + \frac{r+1}{6}$

r can be 5, 35

for $r = 5, k = \pm 2$

$r = 35, k = \pm 3$

Hence number of order pair = 4

9. Let $4\alpha \int_{-1}^2 e^{-\alpha|x|} dx = 5$ then $\alpha =$

A) $\ln 2$

B) $\ln \sqrt{2}$

C) $\ln \frac{3}{4}$

D) $\ln \frac{4}{3}$

Ans. A

$$\begin{aligned} \text{Sol. } 4\alpha \left\{ \int_{-1}^0 e^{\alpha x} dx + \int_{-1}^0 e^{-\alpha x} dx \right\} &= 5 \\ \Rightarrow 4\alpha \left\{ \left(\frac{e^{\alpha x}}{\alpha} \right)_{-1}^0 + \left(\frac{e^{-\alpha x}}{-\alpha} \right)_{-1}^0 \right\} &= 5 \\ \Rightarrow 4\alpha \left\{ \left(\frac{1 - e^{-\alpha}}{\alpha} \right) - \left(\frac{e^{-2\alpha} - 1}{\alpha} \right) \right\} &= 5 \\ \Rightarrow 4(2 - e^{-\alpha} - e^{-2\alpha}) &= 5 \text{ Put } e^{-\alpha} = t \\ \Rightarrow 4t^2 + 4t - 3 &= 0 \\ \Rightarrow (2t + 3)(2t - 1) &= 0 \\ \Rightarrow e^{-\alpha} &= \frac{1}{2} \\ \Rightarrow \alpha &= \ln 2 \end{aligned}$$

10. Let $f(x)$ is a five degree polynomial which has critical points $x = \pm 1$ and $\lim_{x \rightarrow 0} \left(2 + \frac{f(x)}{x^3} \right) = 4$ then which one is incorrect.

- A) $f(x)$ has minima at $x = 1$ & maxima at $x = -1$ B) $f(1) - 4f(-1) = 4$
 C) $f(x)$ is maxima at $x = 1$ and minima $x = -1$ D) $f(x)$ is odd

Ans. A

$$\begin{aligned} \text{Sol. } f(x) &= ax^5 + bx^4 + cx^3 \\ \lim_{x \rightarrow 0} \left(2 + \frac{ax^5 + bx^4 + cx^3}{x^3} \right) &= 4 \Rightarrow 2 + c = 4 \Rightarrow c = 2 \\ f'(x) &= 5ax^4 + 4bx^3 + 6x^2 \\ &= x^2(5ax^2 + 4bx + 6) \\ f'(1) &= 0 \\ \Rightarrow 5a + 4b + 6 &= 0 \\ f'(-1) &= 0 \\ \Rightarrow 5a - 4b + 6 &= 0 \\ b &= 0 \\ a &= -\frac{6}{5} \\ f(x) &= -\frac{6}{5}x^5 + 2x^3 \\ f'(x) &= -6x^4 + 6x^2 \\ &= 6x^2(-x^2 + 1) \\ &= -6x^2(x + 1)(x - 1) \\ &\frac{-1}{1-} + \frac{1}{1-} \\ \text{Minima at } x &= -1 \\ \text{Maxima at } x &= 1 \end{aligned}$$

11. If $\vec{a}, \vec{b}, \vec{c}$ are unit vectors such that $\vec{a} + \vec{b} + \vec{c} = 0$ and $\lambda = \vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a}$ and $\vec{d} = \vec{a} \times \vec{b} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a}$ then $(\lambda, \vec{d}) =$

- A) $\left(\frac{3}{2}, 3\vec{a} \times \vec{b} \right)$ B) $\left(\frac{3}{2}, 3\vec{a} \times \vec{c} \right)$ C) $\left(-\frac{3}{2}, 3\vec{a} \times \vec{c} \right)$ D) $\left(-\frac{3}{2}, 3\vec{a} \times \vec{b} \right)$

Ans. D

$$\begin{aligned} \text{Sol. } |\vec{a} + \vec{b} + \vec{c}|^2 &= 0 \\ 3 + 2(\vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a}) &= 0 \\ (\vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a}) &= \frac{-3}{2} \\ \Rightarrow \lambda &= \frac{-3}{2} \\ \vec{d} &= \vec{a} \times \vec{b} + \vec{b} \times (-\vec{a} - \vec{b}) + (-\vec{a} - \vec{b}) \times \vec{a} \\ &= \vec{a} \times \vec{b} + \vec{a} \times \vec{b} + \vec{a} \times \vec{b} \\ \vec{d} &= 3(\vec{a} \times \vec{b}) \end{aligned}$$

12. Coefficient of x^7 in $(1 + x)^{10} + x(1 + x)^9 + x^2(1 + x)^8 + \dots + x^{10}$ is

- A) 330 B) 210 C) 420 D) 260

Ans. A

Sol. $\frac{(1+x)^{10} \left[1 - \left(\frac{x}{1+x}\right)^{11} \right]}{\left(1 - \frac{x}{1+x}\right)} = \frac{(1+x)^{10} [(1+x)^{11} - x^{11}]}{(1+x)^{11} \times \frac{1}{(1+x)}}$
 $= (1+x)^{11} - x^{11}$
Coefficient of x^7 is ${}^{11}C_7 = {}^{11}C_4 = 330$

13. Let α and β are the roots of $x^2 - x - 1 = 0$ such that $P_k = \alpha^k + \beta^k, k \geq 1$ then which one is incorrect?

- A) $P_5 = P_2 \times P_3$
C) $P_3 = P_5 - P_4$
B) $P_1 + P_2 + P_3 + P_4 + P_5 = 26$
D) $P_4 = 11$

Ans. A

Sol. $\alpha^5 = 5\alpha + 3$
 $\beta^5 = 5\beta + 3$
 $P_5 = 5(\alpha + \beta) + 6$
 $= 5(1) + 6$
 $P_5 = 11$ and $P_5 = \alpha^2 + \beta^2 = \alpha + 1 + \beta + 1$
 $P_2 = 3$ and $P_3 = \alpha^3 + \beta^3 = 2\alpha + 1 + 2\beta + 1 = 2(1) + 2 = 4$
 $P_2 \times P_3 = 12$ and $P_5 = 11 \Rightarrow P_5 \neq P_2 \times P_3$

14. Let $f(x) = x^3 - 4x^2 + 8x + 11$, if LMVT is applicable on $f(x)$ in $[0, 1]$, value of c is:

- A) $\frac{4-\sqrt{7}}{3}$
B) $\frac{4-\sqrt{5}}{3}$
C) $\frac{4+\sqrt{7}}{3}$
D) $\frac{4+\sqrt{5}}{3}$

Ans. A

Sol. $f(x)$ is a polynomial function

\therefore It is continuous and differentiable in $[0, 1]$

Here $f(0) = 11, f(1) = 1 - 4 + 8 + 11 = 16$

$f'(x) = 3x^2 - 8x + 8$

$\therefore f'(c) = \frac{f(1) - f(0)}{1 - 0} = \frac{16 - 11}{1} = 3c^2 - 8c + 8$

$\Rightarrow 3c^2 - 8c + 3 = 0$

$c = \frac{8 \pm 2\sqrt{7}}{6} = \frac{4 \pm \sqrt{7}}{3}$

$\therefore c = \frac{4 - \sqrt{7}}{3} \in (0, 1)$

15. The area bounded by $4x^2 \leq y \leq 8x + 12$ is -

- A) $\frac{127}{3}$
B) $\frac{128}{3}$
C) $\frac{124}{3}$
D) $\frac{125}{3}$

Ans. B

Sol. $4x^2 = y$

$y = 8x + 12$

$4x^2 = 8x + 12$

$x^2 - x - 3 = 0$

$x^2 - 2x - 3 = 0$

$x^2 - 3x + x - 3 = 0$

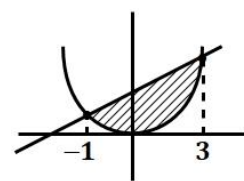
$(x + 1)(x - 3) = 0$

$x = -1$

$A = \int_{-1}^3 (8x + 12 - 4x^2) dx$

$A = \left. \frac{8x^2}{2} + 12x - \frac{4x^3}{3} \right|_{-1}^3 = (4(9) + 36 - 36) - \left(4 - 12 + \frac{4}{3} \right) = 36 + 8 - \frac{4}{3}$

$= 44 - \frac{4}{3} = \frac{132 - 4}{3} = \frac{128}{3}$



16. There are 5 machines. Probability of a machine being faulted is $\frac{1}{4}$. Probability of almost two machines is faulted, is $\left(\frac{3}{4}\right)^3 k$ then value of k is

A) $\frac{17}{2}$ B) 4 C) $\frac{17}{8}$ D) $\frac{17}{4}$

Ans. C

Sol. Required probability = when no. machine has fault + when only one machine has fault + when only two machines have fault.

$$\begin{aligned} &= {}^5C_0 \left(\frac{3}{4}\right)^5 + {}^5C_1 \left(\frac{1}{4}\right) \left(\frac{3}{4}\right)^4 + {}^5C_2 \left(\frac{1}{4}\right)^2 \left(\frac{3}{4}\right)^3 \\ &= \frac{243}{1024} + \frac{405}{1024} + \frac{270}{1024} = \frac{918}{1024} = \frac{459}{512} = \frac{27 \times 17}{64 \times 8} \\ &= \left(\frac{3}{4}\right)^3 \times k = \left(\frac{3}{4}\right)^3 \times \frac{17}{8} \\ \therefore k &= \frac{17}{8} \end{aligned}$$

17. $3x + 4y = 12\sqrt{2}$ is the tangent to the ellipse $\frac{x^2}{a^2} + \frac{y^2}{9} = 1$ then the distance between foci of ellipse is -

A) $1\sqrt{5}$ B) $2\sqrt{3}$ C) $2\sqrt{7}$ D) 4

Ans. C

Sol. $3x + 4y = 12\sqrt{2}$

$$\Rightarrow 4y = -3x + 12\sqrt{2}$$

$$\Rightarrow y = -\frac{3}{4}x + 3\sqrt{2}$$

condition of tangency $c^2 = a^2m^2 + b^2$

$$18 = a^2 \cdot \frac{9}{16} + 9$$

$$a^2 \cdot \frac{9}{16} = 9$$

$$a^2 = 16$$

$$1a = 4$$

$$e = \sqrt{1 - \frac{b^2}{a^2}} = \sqrt{1 - \frac{9}{16}} = \frac{\sqrt{7}}{4}$$

$$\therefore ae = \frac{\sqrt{7}}{4} \cdot 4 = \sqrt{7}$$

$$\therefore \text{focus are } (\pm\sqrt{7}, 0)$$

$$\therefore \text{distance between foci} = 2\sqrt{7}$$

18. If $z = \frac{3+i \sin \theta}{4-i \cos \theta}$ is purely real and $\theta \in \left(\frac{\pi}{2}, \pi\right)$ then $\arg(\sin \theta + i \cos \theta)$ is

A) $-\tan^{-1} \frac{3}{4}$ B) $\pi - \tan^{-1} \frac{3}{4}$ C) $\pi - \tan^{-1} \frac{4}{3}$ D) $\tan^{-1} \frac{4}{3}$

Ans. C

Sol. $z = \frac{(3+i \sin \theta)}{(4-i \cos \theta)} \times \frac{(4+i \cos \theta)}{(4+i \cos \theta)}$

$$\text{as } z \text{ is purely real} \Rightarrow 3 \cos \theta + 4 \sin \theta = 0 \Rightarrow \tan \theta = -\frac{3}{4}$$

$$\arg(\sin \theta + i \cos \theta) = \pi + \tan^{-1} \left(\frac{\cos \theta}{\sin \theta}\right) = \pi + \tan^{-1} \left(-\frac{4}{3}\right) = \pi - \tan^{-1} \left(\frac{4}{3}\right)$$

19. $a_1, a_2, a_3, \dots, a_9$ are in GP where $a_1 < 0$, $a_1 + a_2 = 4$, $a_3 + a_4 = 16$, if $\sum_{i=1}^9 a_i = 4\lambda$, then λ is equal to

A) -513 B) $-\frac{511}{3}$ C) -171 D) 171

Ans. C

$$\text{Sol. } a_1 + a_2 = 4 \Rightarrow a_1 + a_1 r = 4 \quad \text{(i)}$$

$$a_3 + a_4 = 16 \Rightarrow a_1 r^2 + a_1 r^3 = 16 \quad \text{(ii)}$$

$$\frac{1}{r^2} + \frac{1}{4} \Rightarrow r^2 = 4$$

$$r = \pm 2$$

$$r = 2, a_1(1 + 2) = 4 \Rightarrow a_1 = \frac{4}{3}$$

$$r = -2, a_1(1 - 2) = 4 \Rightarrow a_1 = -4$$

$$\sum_{i=1}^a a_i = \frac{a_1(r^a - 1)}{r - 1} = \frac{(-4)((-2)^9 - 1)}{-2 - 1} = \frac{4}{3}(-513) = 4\lambda$$

$$\lambda = -171$$

20. If $y\sqrt{1-x^2} = k - x\sqrt{1-y^2}$ and $y\left(\frac{1}{2}\right) = -\frac{1}{4}$. Then $\frac{dy}{dx}$ at $x = \frac{1}{2}$ is

A) $\frac{2}{\sqrt{5}}$

B) $-\frac{\sqrt{5}}{4}$

C) $-\frac{\sqrt{5}}{2}$

D) $\frac{\sqrt{5}}{2}$

Ans. C

Sol. $x = \frac{1}{2}, y = \frac{-1}{4} \Rightarrow xy = \frac{-1}{8}$

$$y \cdot \frac{1 \cdot (-2x)}{2\sqrt{-x^2}} + y' \cdot \sqrt{1-x^2} = \left\{ 1 \cdot \sqrt{1-y^2} + \frac{x \cdot (-2y)}{2\sqrt{1-y^2}} y' \right\}$$

$$-\frac{xy}{\sqrt{1-x^2}} + y' \sqrt{1-x^2} = -\sqrt{1-y^2} + \frac{xy \cdot y'}{\sqrt{1-y^2}}$$

$$y' \left(\sqrt{1-x^2} - \frac{xy}{\sqrt{1-y^2}} \right) = \frac{xy}{\sqrt{1-x^2}} - \sqrt{1-y^2}$$

$$y' \left(\frac{\sqrt{3}}{2} + \frac{1}{8 \cdot \frac{\sqrt{15}}{4}} \right) = \frac{-1}{8 \cdot \frac{\sqrt{3}}{2}} - \frac{\sqrt{15}}{4}$$

$$y' \left(\frac{\sqrt{45} + 1}{2\sqrt{15}} \right) = -\frac{(1 + \sqrt{45})}{4\sqrt{3}}$$

$$y' = -\frac{\sqrt{5}}{2}$$

21. Let $X = \{x : 1 \leq x \leq 50, x \in N\}$

$A = \{x : x \text{ is multiple of } 2\}$

$B = \{x : x \text{ is multiple of } 7\}$

Then find number of elements in the smallest subset of X which contain elements of both A and B

Ans. 29

Sol. $n(A \cup B) = n(A) + n(B) - n(A \cap B)$
 $= 25 + 7 - 3$
 $= 29$

22. If $Q\left(\frac{5}{3}, \frac{7}{3}, \frac{17}{3}\right)$ is foot of perpendicular drawn from $P(1, 0, 3)$ on a line L and if line L is passing through $(\alpha, 7, 1)$, then value of α is

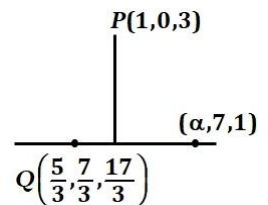
Ans. 4

Sol. Since PQ is perpendicular to L , therefore

$$\left(1 - \frac{5}{3}\right)\left(\alpha - \frac{5}{3}\right) + \left(\frac{-7}{3}\right)\left(7 - \frac{7}{3}\right) + \left(3 - \frac{17}{3}\right)\left(1 - \frac{17}{3}\right) = 0$$

$$\Rightarrow \frac{-2\alpha}{3} + \frac{10}{9} - \frac{98}{9} + \frac{112}{9} = 0$$

$$\Rightarrow \frac{2\alpha}{3} = \frac{24}{9} \Rightarrow \alpha = 4$$



23. If $f(x)$ is defined in $x \in \left(-\frac{1}{3}, \frac{1}{3}\right)$

$$f(x) = \begin{cases} \left(\frac{1}{x}\right) \log_e \left(\frac{1+3x}{1-2x}\right) & x \neq 0 \\ k & x = 0 \end{cases}$$

Find k such that $f(x)$ is continuous

Ans. 5

Sol. $\lim_{x \rightarrow 0} f(x) = \lim_{x \rightarrow 0} \left(\frac{1}{x} \ln \left(\frac{1+3x}{1-2x} \right) \right) = \lim_{x \rightarrow 0} \left(\frac{\ln(1+3x)}{x} - \frac{\ln(1-2x)}{x} \right)$
 $= \lim_{x \rightarrow 0} \left(\frac{3 \ln(1+3x)}{3x} - \frac{2 \ln(1-2x)}{-2x} \right) = 3 + 2 = 5$
 $\therefore f(x)$ will be continuous $f(0) = \lim_{x \rightarrow 0} f(x)$

24. If system of equation

$$x + y + z = 6$$

$$x + 2y + 3z = 10$$

$$3x + 2y + \lambda z = \mu$$

Has more than two solutions. Find $(\mu - \lambda^2)$

Ans. 13

Sol. $x + y + z = 6$ (1)

$$x + 2y + 3z = 10$$
 (2)

$$3x + 2y + \lambda z = \mu$$
 (3)

From (1) and (2)

$$\text{If } z = 0 \Rightarrow x + y = 6 \text{ and } x + 2y = 10$$

$$\Rightarrow y = 4, x = 2$$

$$(2, 4, 0)$$

$$\text{If } y = 0 \Rightarrow x + z = 6 \text{ and } x + 3z = 10$$

$$\Rightarrow z = 2 \text{ and } x = 4$$

$$(4, 0, 2)$$

$$\text{So } 3x + 2y + \lambda z = \mu$$

Must pass through $(2, 4, 0)$ and $(4, 0, 2)$

$$\text{So } 6 + 8 = \mu \Rightarrow \mu = 14$$

$$\text{And } 12 + 2\lambda = \mu$$

$$12 + 2\lambda = 14 \Rightarrow \lambda = 1$$

$$\text{So } \mu - \lambda^2 = 14 - 1$$

$$= 13$$

25. If mean and variance of 2, 3, 16, 20, 13, 7, x , y are 10 and 25 respectively then find xy

Ans. 124

Sol. Mean $= \bar{x} = \frac{2+3+16+20+13+7+x+y}{8} = 10 \Rightarrow x + y = 19$ (1)

$$\text{Variance } \sigma^2 = \frac{\sum(x_i)^2}{8} - (\bar{x})^2 = 25$$

$$\frac{4 + 9 + 256 + 400 + 169 + 49 + x^2 + y^2}{8} - 100 = 25$$

$$\Rightarrow x^2 + y^2 = 113$$
 (2)

$$(x + y)^2 = (19)^2 \Rightarrow x^2 + y^2 + 2xy = 361 \Rightarrow xy = 124$$

(exact data is not retrieved so ans. can vary)